

Study of HWRD process $\Xi^0 \rightarrow \Sigma^0 \gamma$

Jiajun Tang

University of Science and Technology of China

Apr 3, 2023

Motivation

Hara theorem

In hyperon weak radiative decay(HWRD):

B^{PV} should vanish under SU(3) limit $\rightarrow \alpha_\gamma = 0$

Take the weak breaking of SU(3) symmetry into consideration $\alpha_\gamma \sim \pm 0.2$

$$\alpha_\gamma = \frac{2\text{Re}(A^{PC} * B^{PV})}{|A^{PC}|^2 + |B^{PV}|^2}$$

- α_γ : decay asymmetry
- A^{PC} : parity conserving amplitude
- B^{PV} : parity violating amplitude

Motivation

Measurements of decay asymmetry for $\Xi^0 \rightarrow \Sigma \gamma$

Experiments	BR/ 10^{-3}	α	Events
1989 SPEC	$3.56 \pm 0.42 \pm 0.10$	$+0.20 \pm 0.32 \pm 0.05$	85
2000 NA48	$3.16 \pm 0.76 \pm 0.32$	—	17
2001 KTEV	$3.34 \pm 0.05 \pm 0.09$	$-0.63 \pm 0.08 \pm 0.05$	4045
2010 NA48	—	$-0.729 \pm 0.030 \pm 0.076$	15k

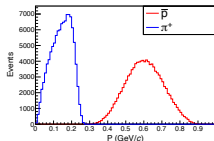
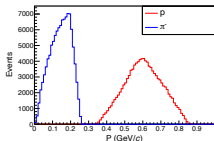
Analysis Strategy

$$J/\psi \rightarrow \Xi^0 \bar{\Xi}^0, \bar{\Xi}^0 \rightarrow \bar{\Sigma}^0 \gamma, \Xi^0 \rightarrow \Lambda \pi^0, \bar{\Sigma}^0 \rightarrow \bar{\Lambda} \gamma$$

Full Reconstruction

Charged Tracks

- $\cos \theta < 0.93$
- $N \geq 4$
- PID
 - p: $P_p > 0.3 \text{ GeV}$ && $\text{Prob}(p) > \text{Prob}(K)$,
 $\text{Prob}(p) > \text{Prob}(\pi)$
 - π : $P_\pi < 0.3 \text{ GeV}$
- $N_p, N_{\pi^-}, N_{\bar{p}}, N_{\pi^+} \geq 1$



- $\Lambda \bar{\Lambda}$: Primary vertex fit, loop $p\pi^- (\bar{p}\pi^+)$ pairs to find the best (no χ^2 requirement)

Neutral Tracks

- Angle between n.t. and c.t. ($\bar{p}$) larger than 10° (20°)
- $25 \text{ MeV} @ |\cos \theta| < 0.8$ && $50 \text{ MeV} @ 0.86 < |\cos \theta| < 0.92$ && $0 \leq \text{TDC} \leq 14$
- $N_\gamma \geq 4$
- 1C get a set of π^0 ($\chi^2_{\pi^0} < 20$)

Kinematics Fit(7C)

- Constrain m_{Ξ^-}, m_{Ξ}
- Loop π^0 and $\gamma\gamma$ pairs to optimize

Main BKG KF(8C) && $\Lambda \bar{\Lambda}$ 2nd VF

Feasibility analysis – Generator

Decay amplitude

$$\mathcal{W} = \sum_{\mu, \nu=0}^3 C_{\mu\nu} \sum_{\mu', \nu', \rho=0}^3 a_{\mu\mu'}^{\Xi} a_{\nu\nu'}^{\bar{\Xi}} a_{\mu'0}^{\Lambda} a_{\nu'\rho}^{\bar{\Sigma}} a_{\rho0}^{\bar{\Lambda}} \quad (1)$$

For $1 \rightarrow \frac{1}{2} + \frac{1}{2}$ decay ($J/\psi \rightarrow \Xi^0 \bar{\Xi}^0$)

For $\frac{1}{2} \rightarrow \frac{1}{2} + 1$ decay ($\bar{\Xi}^0 \rightarrow \bar{\Sigma} \gamma, \bar{\Sigma} \rightarrow \bar{\Lambda} \gamma$)

$$C_{\mu\nu} = \begin{pmatrix} 1 + \alpha_{\psi} \cos^2 \theta & 0 & \beta_{\psi} \sin \theta \cos \theta & 0 \\ 0 & \sin^2 \theta & 0 & \gamma_{\psi} \sin \theta \cos \theta \\ -\beta_{\psi} \sin \theta \cos \theta & 0 & \alpha_{\psi} \sin^2 \theta & 0 \\ 0 & -\gamma_{\psi} \sin \theta \cos \theta & 0 & -(\alpha_{\psi} + \cos^2 \theta) \end{pmatrix} \quad (2)$$

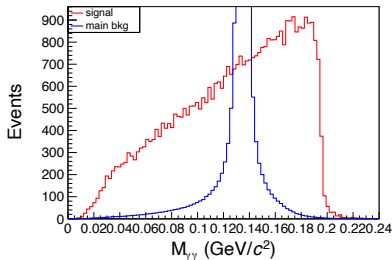
$$a_{\nu\nu'} = \begin{pmatrix} 1 & 0 & 0 & -\alpha \\ \alpha \cos \phi \sin \theta & 0 & 0 & -\cos \phi \sin \theta \\ \alpha \sin \theta \sin \phi & 0 & 0 & -\sin \theta \sin \phi \\ \alpha \cos \theta & 0 & 0 & -\cos \theta \end{pmatrix}$$

For $\frac{1}{2} \rightarrow \frac{1}{2} + 0$ decay ($\Xi^0 \rightarrow \Lambda \pi^0, \Lambda \rightarrow p \pi$)

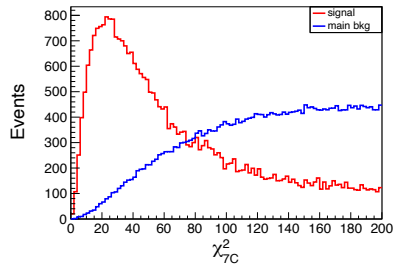
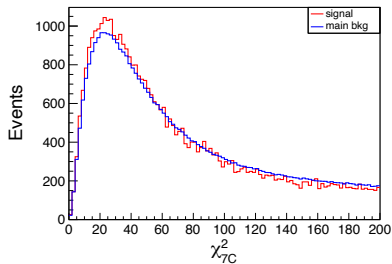
$$a_{\mu\mu'} = \begin{pmatrix} 1 & 0 & 0 & \alpha \\ \alpha \cos \phi \sin \theta & \gamma \cos \phi \cos \theta - \beta \sin \phi & -\beta \cos \phi \cos \theta - \gamma \sin \phi & \cos \phi \sin \theta \\ \alpha \sin \phi \sin \theta & \beta \cos \phi + \gamma \cos \theta \sin \phi & \gamma \cos \phi - \beta \cos \theta \sin \phi & \sin \phi \sin \theta \\ \alpha \cos \theta & -\gamma \sin \theta & \beta \sin \theta & \cos \theta \end{pmatrix} \quad (3)$$

Feasibility analysis – Further Selection

- 600,000 Signal MC
- 21,000,000 Main Background MC



$$0.115 < M_{\gamma\gamma} < 0.15$$



$$\chi^2_{7C} < 40$$

Feasibility analysis – Event Level BDT

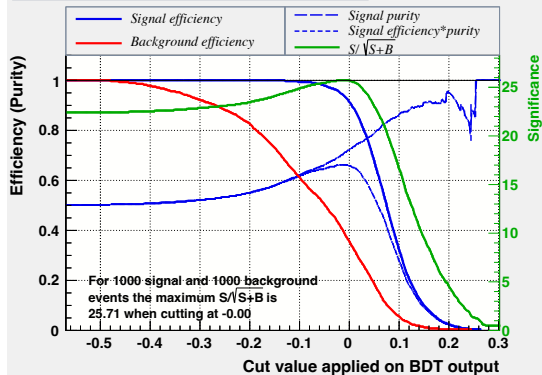
$$J/\psi \rightarrow \Xi^0 \bar{\Xi}^0, \bar{\Xi}^0 \rightarrow \bar{\Sigma}^0 \gamma(\gamma 2), \Xi^0 \rightarrow \Lambda \pi^0, \bar{\Sigma}^0 \rightarrow \bar{\Lambda} \gamma(\gamma 1)$$

- Input Sample: Signal(11918) & Main BKG(6909) MC after further selection
- Input Variables:

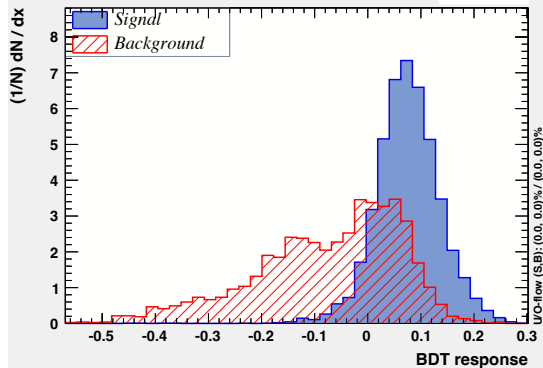
$$\gamma 1, \gamma 2's E, \text{ shower shape, } \cos \theta \text{ \& } \bar{\Lambda}'s p, \cos \theta(cms)$$

Feasibility analysis – Event Level BDT

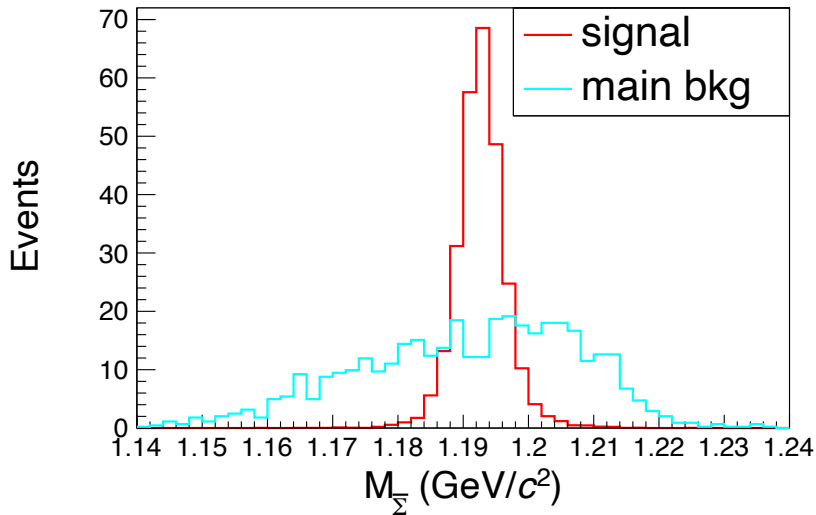
Cut efficiencies and optimal cut value



TMVA response for classifier: BDT



Feasibility analysis – Event Level BDT



Normalize to 10 billion J/ψ
(not include charge conjugate
channel)

$$N_{sig} \doteq 273$$

$$N_{mbkg} \doteq 383$$

Feasibility analysis – Cutflow

Criteria	Signal MC			Main Bkg MC		
	Events	Relative Effi	Effi	Events	Relative Effi	Effi
NTotal	600000	-	-	21000000	-	-
Good Charged Track	318822	53.14%	53.14%	11050400	52.62%	52.62%
PID for $p\pi^-$	243234	76.29%	40.54%	8403188	76.04%	40.02%
Vertex Fit for Λ	220109	90.49%	36.68%	7618629	90.67%	36.28%
γ	170321	77.38%	28.39%	5802051	76.16%	27.63%
KF	40996	24.07%	6.83%	1414786	24.38%	6.74%
$M_{\gamma\gamma}$	30895	75.36%	5.15%	172618	12.20%	0.82%
χ^2_{7C}	12003	38.85%	2.00%	7696	4.46%	0.037%
Event-Level BDT	10318	85.96%	1.72%	1697	22.05%	0.008%
Relative Efficiency	215 times					

Bkg analysis – Topology

12, 18 inclusive

Table 1: Decay trees and their respective initial-final states.

rowNo	decay tree (decay initial-final states)	iDecyTr	iDecyIFSts	nEtr	nCEtr
1	$J/\psi \rightarrow \Xi^0 \bar{\Xi}^0, \Xi^0 \rightarrow \pi^0 \Lambda, \bar{\Xi}^0 \rightarrow \pi^0 \bar{\Lambda}, \Lambda \rightarrow \pi^- p, \bar{\Lambda} \rightarrow \pi^+ \bar{p}$ ($J/\psi \rightarrow \pi^0 \pi^0 \pi^+ \pi^- p \bar{p}$)	0	0	879	879
2	$J/\psi \rightarrow \Sigma^{*0} \bar{\Sigma}^{*0}, \Sigma^{*0} \rightarrow \pi^0 \Lambda, \bar{\Sigma}^{*0} \rightarrow \pi^0 \bar{\Lambda}, \Lambda \rightarrow \pi^- p, \bar{\Lambda} \rightarrow \pi^+ \bar{p}$ ($J/\psi \rightarrow \pi^0 \pi^0 \pi^+ \pi^- p \bar{p}$)	3	0	55	934
3	$J/\psi \rightarrow \pi^0 \Sigma^0 \bar{\Sigma}^0, \Sigma^0 \rightarrow \Lambda \gamma, \bar{\Sigma}^0 \rightarrow \bar{\Lambda} \gamma, \Lambda \rightarrow \pi^- p, \bar{\Lambda} \rightarrow \pi^+ \bar{p}$ ($J/\psi \rightarrow \pi^0 \pi^+ \pi^- p \bar{p} \gamma \gamma$)	1	1	49	983
4	$J/\psi \rightarrow \Sigma^0 \Sigma^{*0}, \Sigma^0 \rightarrow \Lambda \gamma, \Sigma^{*0} \rightarrow \pi^0 \Lambda, \bar{\Lambda} \rightarrow \pi^+ \bar{p}, \Lambda \rightarrow \pi^- p$ ($J/\psi \rightarrow \pi^0 \pi^+ \pi^- p \bar{p} \gamma$)	2	2	5	988
5	$J/\psi \rightarrow \Sigma^0 \Sigma^{*0}, \Sigma^0 \rightarrow \Lambda \gamma, \Sigma^{*0} \rightarrow \pi^0 \bar{\Lambda}, \bar{\Lambda} \rightarrow \pi^- p, \bar{\Lambda} \rightarrow \pi^+ \bar{p}$ ($J/\psi \rightarrow \pi^0 \pi^+ \pi^- p \bar{p} \gamma$)	5	2	5	993
6	$J/\psi \rightarrow \pi^0 \Lambda \Sigma^{*0}, \bar{\Lambda} \rightarrow \pi^+ \bar{p}, \Sigma^{*0} \rightarrow \pi^0 \Lambda, \Lambda \rightarrow \pi^- p$ ($J/\psi \rightarrow \pi^0 \pi^0 \pi^+ \pi^- p \bar{p}$)	6	0	4	997
7	$J/\psi \rightarrow \Xi^0 \bar{\Xi}^0, \Xi^0 \rightarrow \pi^0 \Lambda, \bar{\Xi}^0 \rightarrow \pi^0 \bar{\Lambda}, \Lambda \rightarrow \pi^- p, \bar{\Lambda} \rightarrow \pi^+ \bar{p} \gamma'$ ($J/\psi \rightarrow \pi^0 \pi^0 \pi^+ \pi^- p \bar{p} \gamma'$)	13	4	3	1000
8	$J/\psi \rightarrow \eta_c \gamma, \eta_c \rightarrow \Xi^0 \bar{\Xi}^0, \Xi^0 \rightarrow \pi^0 \Lambda, \bar{\Xi}^0 \rightarrow \pi^0 \bar{\Lambda}, \Lambda \rightarrow \pi^- p, \bar{\Lambda} \rightarrow \pi^+ \bar{p}$ ($J/\psi \rightarrow \pi^0 \pi^0 \pi^+ \pi^- p \bar{p} \gamma$)	22	8	3	1003
9	$J/\psi \rightarrow \Sigma^{*+} \bar{\Sigma}^{*-}, \Sigma^{*+} \rightarrow \pi^0 \Sigma^+, \bar{\Sigma}^{*-} \rightarrow \pi^- \bar{\Lambda}, \Sigma^+ \rightarrow \pi^0 p, \bar{\Lambda} \rightarrow \pi^+ \bar{p}$ ($J/\psi \rightarrow \pi^0 \pi^0 \pi^+ \pi^- p \bar{p}$)	16	0	2	1005

$$J/\psi \rightarrow \Xi^0 \bar{\Xi}^0, \Xi^0 \rightarrow \pi^0 \Lambda, \bar{\Xi}^0 \rightarrow \pi^0 \bar{\Lambda}, \Lambda \rightarrow \pi^- p, \bar{\Lambda} \rightarrow \pi^+ \bar{p} (879)$$

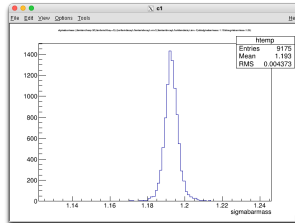
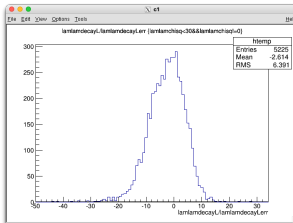
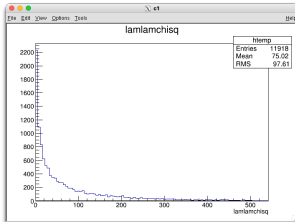
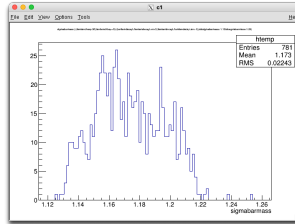
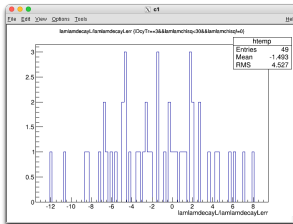
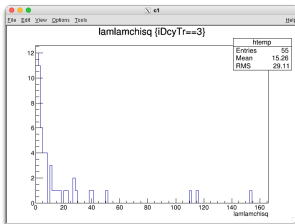
$$J/\psi \rightarrow \Sigma^{*0} \bar{\Sigma}^{*0}, \Sigma^{*0} \rightarrow \pi^0 \Lambda, \bar{\Sigma}^{*0} \rightarrow \pi^0 \bar{\Lambda}, \Lambda \rightarrow \pi^- p, \bar{\Lambda} \rightarrow \pi^+ \bar{p} (55)$$

$$J/\psi \rightarrow \pi^0 \Sigma^0 \bar{\Sigma}^0, \Sigma^0 \rightarrow \Lambda \gamma, \bar{\Sigma}^0 \rightarrow \bar{\Lambda} \gamma, \Lambda \rightarrow \pi^- p, \bar{\Lambda} \rightarrow \pi^+ \bar{p} (49)$$

Bkg analysis – Suppress 2nd bkg

For remaining part

Result



Keep $\chi^2 > 30 \& \chi^2 = 0$

Keep $L/\sigma_L > 3, L/\sigma_L < -6$

Efficiency: 75.94% : 76.98%

Backup

Cutflow of previous version of ana program

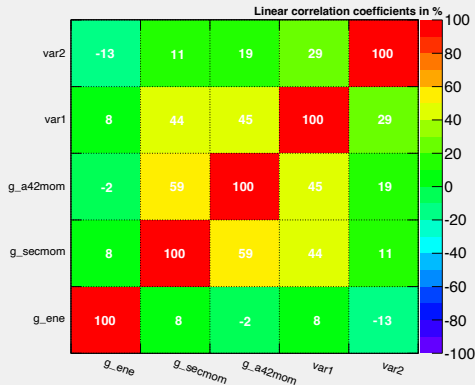
Criteria	Signal MC			Main Bkg MC		
	Events	Relative Effi	Effi	Events	Relative Effi	Effi
NTotal	600000	-	-	3000000	-	-
Good Charged Track	318822	53.14%	53.14%	1713931	57.13%	57.13%
PID for $p\pi^-$	243234	76.29%	40.54%	1326980	77.42%	44.23%
Vertex Fit for Λ	146471	60.22%	24.41%	794247	59.85%	26.47%
γ	42483	29.00%	7.08%	201602	25.38%	6.72%
KF	10067	23.70%	1.68%	47477	23.55%	1.58%
$M_{\gamma\gamma}$	7647	75.96%	1.27%	4202	8.85%	0.14%
χ^2_{7C}	3354	43.86%	0.56%	150	3.57%	0.005%
Event-Level BDT	3167	94.42%	0.53%	47	33.10%	0.0015%
Relative Efficiency	337 times					

Cutflow of latest version of ana program

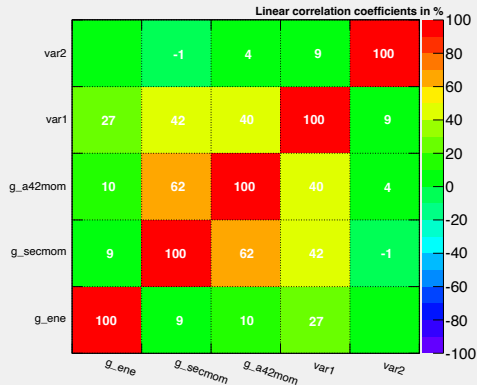
Criteria	Signal MC			Main Bkg MC		
	Events	Relative Effi	Effi	Events	Relative Effi	Effi
NTotal	600000	-	-	21000000	-	-
Good Charged Track	318822	53.14%	53.14%	11050400	52.62%	52.62%
PID for $p\pi^-$	243234	76.29%	40.54%	8403188	76.04%	40.02%
Vertex Fit for Λ	220109	90.49%	36.68%	7618629	90.67%	36.28%
γ	170321	77.38%	28.39%	5802051	76.16%	27.63%
KF	40996	24.07%	6.83%	1414786	24.38%	6.74%
$M_{\gamma\gamma}$	30895	75.36%	5.15%	172618	12.20%	0.82%
χ^2_{7C}	12003	38.85%	2.00%	7696	4.46%	0.037%
Event-Level BDT	10318	85.96%	1.72%	1697	22.05%	0.008%
Relative Efficiency	215 times					

Backup – Track Level BDT

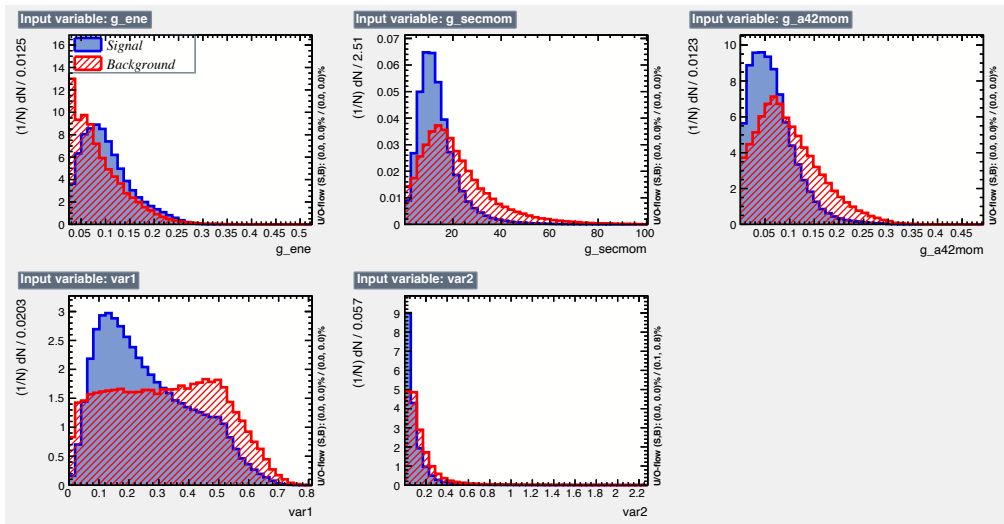
Correlation Matrix (signal)



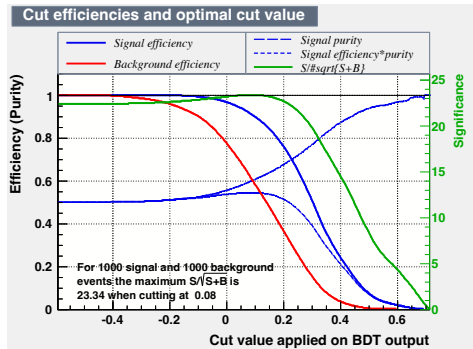
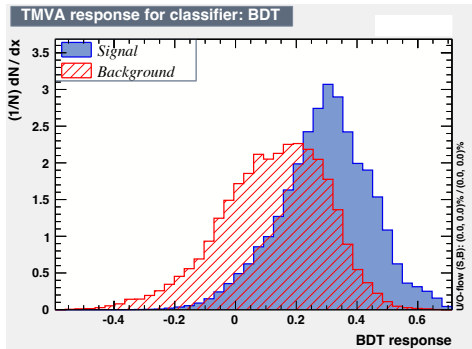
Correlation Matrix (background)



Backup – Track Level BDT



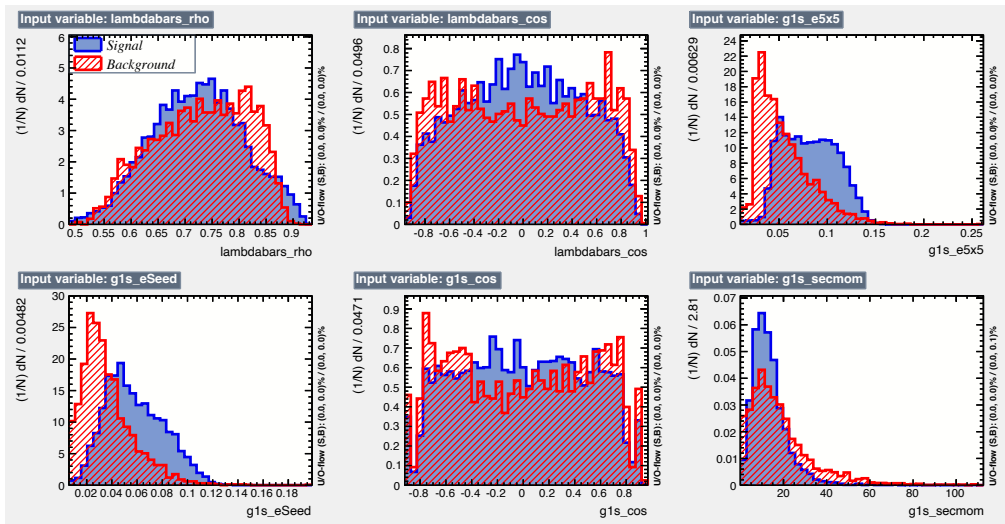
Backup – Track Level BDT



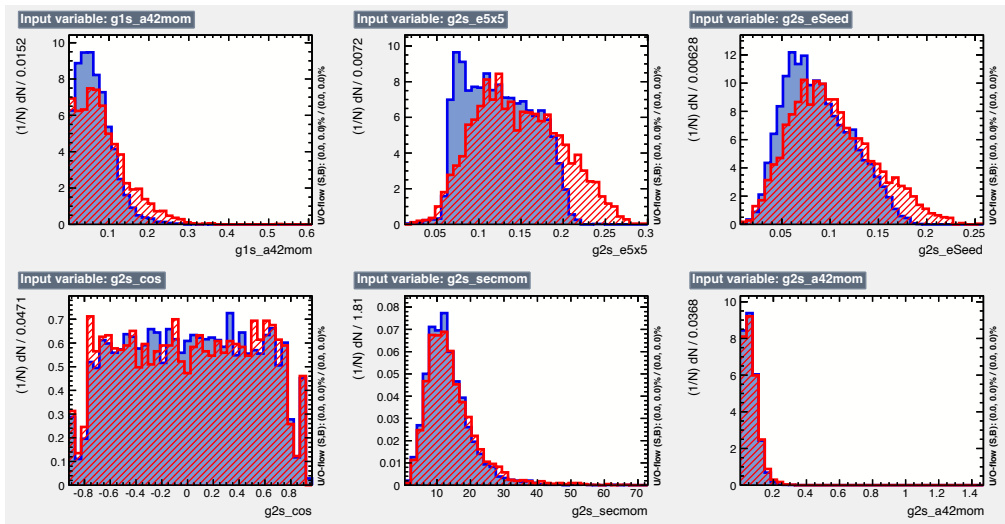
Backup – Event Level BDT

```
--- BDT : -----  
--- BDT : Rank : Variable           : Variable Importance  
--- BDT : -----  
--- BDT : 1 : g1s_e5x5             : 1.247e-01  
--- BDT : 2 : g2s_e5x5             : 1.212e-01  
--- BDT : 3 : lambdabars_rho       : 8.379e-02  
--- BDT : 4 : lambdabars_cos      : 8.149e-02  
--- BDT : 5 : g1s_cos_cms        : 7.167e-02  
--- BDT : 6 : g2s_eSeed           : 6.962e-02  
--- BDT : 7 : g1s_eSeed           : 6.324e-02  
--- BDT : 8 : g1s_cos             : 6.201e-02  
--- BDT : 9 : g2s_cos             : 5.977e-02  
--- BDT : 10 : lambdabars_cos_cms : 5.963e-02  
--- BDT : 11 : g1s_secmom         : 5.826e-02  
--- BDT : 12 : g1s_a42mom        : 4.991e-02  
--- BDT : 13 : g2s_a42mom        : 4.890e-02  
--- BDT : 14 : g2s_secmom        : 4.585e-02  
--- BDT : -----
```

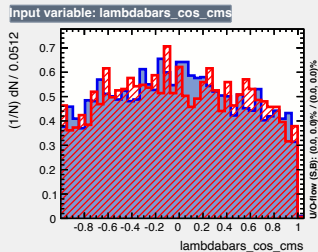
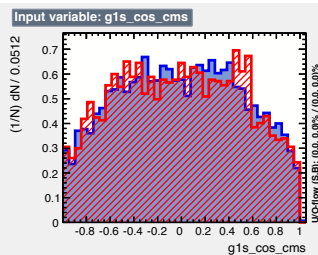
Backup – Event Level BDT



Backup – Event Level BDT

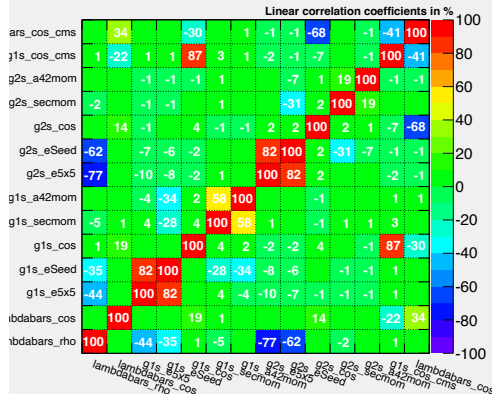


Backup – Event Level BDT



Backup – Event Level BDT

Correlation Matrix (signal)



Correlation Matrix (background)

