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# Observation of a resonant structure in the cross section of $e^+e^- \rightarrow \phi \eta'$ at center-of-mass energies between 2.050 and 3.080 GeV

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Based on data samples collected with the BESIII detector at the BEPCII collider at 22 center of mass energies from 2.0 to 3.08 GeV, we search for the production of  $e^+e^- \rightarrow \phi \eta'$ . The Born cross sections of  $e^+e^- \rightarrow \phi \eta'$  process are observed for the first time. Assuming the  $\phi \eta'$  signals from a single resonance, we extract the mass and width of the resonance to be (2182.4 ± 5.1 ± 1.6) MeV/ $c^2$  and (142.2 ± 16.6 ± 0.0) MeV, respectively, and the statistical significance is more than  $12\sigma$ .

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### I. INTRODUCTION

The  $\phi(2170)$  resonance was first discovered in the process  $e^+e^- \rightarrow \phi f_0(980)$  by the BABAR [1] via initialstate radiation (ISR) technique and then confirmed by Belle [2]. BES [3] and BESIII [4, 5] also observed the 9  $\phi(2170)$  in the  $\phi f_0(980)$  invariant mass spectrum. The 10 state does not fit into the conventional strangenium spec-11 trum of the quark model. In addition, even though the 12 mass of the  $\phi(2170)$  is well above the  $K\bar{K}$  threshold, it 48 13 has not yet been found to decay to  $K\bar{K}$  [6], in contrast to 49 14 the conventional strangenium states in this mass region.  $_{50}$ 15

There are several theoretical interpretations of <sup>51</sup> 16  $\phi(2170)$ , including a  $s\overline{s}g$  hybrid [7, 8], a  $2^3D_1$  [9] or <sub>52</sub> 17  $3^{3}S_{1}$  ss [10], a tetraquark state [11, 12], a  $\Lambda\overline{\Lambda}$  bound <sub>53</sub> 18 state [13, 14], an S-wave threshold effects [15], or a three-19 meson system  $\phi K^+ K^-$  [16]. The  $3^3 S_1 s \bar{s}$  state is pre-20 dicted to have significant branching fractions to the  $s\bar{s}$ -21 signature modes  $\phi \eta$  and  $\phi \eta'$ , whereas the decay couplings <sub>57</sub> 22 of any  $n\bar{n}$  (where  $n\equiv u$ , d) state to anything +  $\phi$  should <sub>58</sub> 23 be weak. Although the  $\phi \eta'$  mode of the hybird should <sub>59</sub> 24 be weak, the  $s\bar{s}$ -hybrid vector should also have a large 25  $\phi\eta$  branching fraction [10]. The different decay modes 26 of  $2^{3}D_{1}$  ss state had been studied [9]. There are signifi-27 cant difference between two modes' width. The  $\phi\eta$  mode  $^{\rm 60}$ 28 should be useful in establishing the true mass and width 29 of the  $3^3S_1s\bar{s}$  state, since interference with nonstrange vectors should be unimportant in this channel. The pre-30 31 diction of a branching fraction ratio of  $B_{\phi(2170)\to\phi\eta/\phi\eta'}^{62}$  should be reliable, as shown in the Table I.  $\phi(2170)$  dom-32 33 in antly decays into  $\phi\eta$  and  $\phi\eta'$  in the tetraquark picture  $^{64}$ 34 under the assumption that the tetraquark prefers to re-  $^{\rm 65}$ 35 arrange into two mesons, so the processes of  $e^+e^- \to \eta \phi$   $^{66}$ 36 and  $e^+e^- \rightarrow \eta' \phi$  also provides a good opportunity to  $^{67}$ 37 study strangeonium vector states above the  $K\bar{K}$  produc-38 69 tion threshold. 39 70

BABAR Collaboration has measured the cross section 71 40 of  $e^+e^- \rightarrow \gamma \phi \eta$  via the initial-state radiation process and 72 41 observed a structure at 2.13 GeV [18]. In a study of ISR 73 42 events of the type,  $e^+e^- \rightarrow \gamma_{ISR}\eta'\phi$ , the BABAR Col-74 43 laboration observed several signal events [19]. Because of 75 44 the low statistics for  $e^+e^- \rightarrow \gamma_{ISR} \eta' \phi$ , they did not carry 76 45 out further study. BESIII has studied of  $J/\psi \rightarrow \phi \eta \eta'$  77 46 decay and reported the observation of the structure at 78 47

TABLE I: The partial decay width of Y(2175) decay as  $2^3D_1$  and  $3^3S_1s\bar{s}$  and  $1^{--}s\bar{s}g$  in the  ${}^3P_0$  model and flux tube model.

Decay Modes	$1^{}s\bar{s}g$ [7]	$2^{3}D_{1}s$	$3^3S_1s\bar{s}$ [10]	
	Flux tube	${}^{3}P_{0}$ model	flux tube	${}^{3}P_{0}$ model
$\phi \eta$	1.2	0	0	21
$\phi \eta'$	0.4	2.9	2.8	11
$B_{\phi\eta/\phi\eta'}$	3	0	0	1.9

2.002 GeV/ $c^2$  by assuming the  $J^P$  value of the structure as 1<sup>-</sup> [17]. Experimental study of  $e^+e^- \rightarrow \phi \eta'$  with large data samples in this energy region may shed light on the nature of the  $\phi(2170)$  state.

The analysis is based on a data sample of 650  $pb^{-1}$  collected at the Beijing spectrometer (BESIII) with centerof-mass energies (c.m. energies) ranging from 2.0 to 3.08 GeV to measure the Born cross sections of the reactions  $e^+e^- \rightarrow \phi \eta'$ . To identify whether or nor the  $\phi \eta'$  system originates from a  $\phi(2170)$ , the energy dependence of the  $e^+e^- \rightarrow \phi \eta'$  cross section is compared to that of  $\phi f_0(980)$ .

#### **II. DETECTOR AND DATA SAMPLES**

The BESIII detector is a magnetic spectrometer [20] located at the Beijing Electron Position Collider (BEPCII) [21]. The cylindrical core of the BE-SIII detector consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muon identifier modules interleaved with steel. The acceptance of charged particles and photons is 93% over  $4\pi$  solid angle. The chargedparticle momentum resolution at 1 GeV/c is 0.5%, and the dE/dx resolution is 6% for the electrons from Bhabha scattering. The EMC measures photon energies with a resolution of 2.5% (5%) at 1 GeV in the barrel (end cap) region. The time resolution of the TOF barrel part is 68 ps, while that of the end cap part is 110 ps.

The optimization of selection criteria, the determina-129 79 tion of detection efficiencies and estimations of potential<sub>130</sub> 80 backgrounds are performed based on Monte Carlo (MC)<sub>131</sub> 81 simulations taking the various aspects of the experimen-132 82 tal setup into account. A GEANT4-based [22] MC sim-133 83 ulation software, which includes geometric and material134 84 description of the BESIII detector, the detector response<sub>135</sub> 85 and digitisation models, as well as accounting of the de-136 86 tector running conditions and performances, is used to 87 137 generate the MC samples. 88

138 For the background study, the process of  $e^+e^- \to q\bar{q}_{_{\rm 139}}$ 89 is simulated by the MC event generator CONEXC [23], 90 while the decays are generated by EVTGEN [24, 25] for140 91 known decay modes with branching fractions set to Par-141 92 ticle Data Group (PDG) world average values [26] and<sup>142</sup> 93 by LUARLW [27] for the remaining unknown decays. The 94 signal MC samples from  $e^+e^- \rightarrow \phi \eta'$  is generated at c.m. 95 energies corresponding to the experimental values, where 96 the line shape of the production cross section of the  $\text{pro-}_{145}$ 97 cess is taken from the BABAR experiment [18]. 98

III. EVENT SELECTION

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For the process  $e^+e^- \rightarrow \phi \eta'$ , the  $\phi$  candidate is reconstructed with  $K^+K^-$  and the  $\eta'$  is via  $\pi^+\pi^-\gamma$  decay<sub>149</sub> mode. Candidate events are required to have three or<sub>150</sub> four charged tracks and at least one photon candidates. <sub>151</sub>

- Good charged tracks: Charged tracks are recon-<sup>153</sup> structed from hits in the MDC within the polar<sup>154</sup> angle range  $|\cos \theta| < 0.93$ . The tracks are required<sup>155</sup> to pass the interaction point within 10 cm along<sup>156</sup> the beam direction and within 1 cm in the plane<sup>157</sup> perpendicular to the beam.
- Particle identification: For each charged track, the<sub>160</sub> TOF and the dE/dx information combined to form<sub>161</sub> particle identification confidence levels (C.L.) for<sub>162</sub> the  $\pi$ , K, and p hypotheses, and the particle type<sub>163</sub> with the highest C.L. is assigned to each track. At least one kaon is required to be identified.
- Good photon: Photon candidate is reconstructed<sup>164</sup> 116 from isolated showers in the EMC, and the cor-165 117 responding energies are required to be at least 25 118 MeV in the barrel  $(|\cos \theta| < 0.80)$  or 50 MeV in 119 the end caps  $(0.86 < |\cos \theta| < 0.92)$ . To elimi-120 nate showers associated with charged particles, the 121 angle between the cluster and the nearest charged 122 track must be larger than 10 degrees. An EMC 123 cluster timing requirement of 0 < t < 700 ns is also 124 applied to suppress electronic noise and energy de-125 posits unrelated to the event. 126
- Vertex fit : The primary vertex of the event is re-168 constructed by two pions and one kaon. 169

- One-constraint (1C) kinematic fit : 1C kinematic fit is performed under the hypothesis that the  $K\pi^+\pi^-\gamma$  missing mass corresponds to the kaon mass. For events with two reconstructed and identified kaons, the combination with the smallest chisquare of 1C kinematic fit is retained. The corresponding  $\chi^2$ , denoted as  $\chi^2_{1C}(\pi^+\pi^-KK_{miss}\gamma)$ , is required to be less than 20.
- Mass window of  $\phi$ : The candidate event is required to be within the  $\phi$  signal region, defined as  $|M(K^+K^-) M_{\phi}| < 0.015$  GeV.
- Energy of photon : In order to suppress the background processes, the energy of photons is required to be larger than 70 MeV.

After applying the above selection criteria, the momentum distributions are shown in Fig. 1, where the  $M(K^+K^-)$  is required to be in the  $\phi$  mass range,  $|M(K^+K^-)-m_{\phi}| < 0.01 GeV/c^2$ , and  $m_{\phi}$  is the nominal  $\phi$  mass from PDG [26].

### **IV. SIGNAL YIELDS**

The signal yields of  $e^+e^- \rightarrow \phi \eta'$  are observed from unbinned maximum likelihood fits to the  $\pi^+\pi^-\gamma$  invariantmass spectrum. The signal is described by the line shape obtained from the MC simulation convoluted with a Gaussian function, which account for the difference in resolution between data and MC simulation. The background shape is parametrized by a second-order polynomial function. The parameters of the Gaussian function and the polynomial function are left free in the fit. The corresponding fit result is shown in Fig. 2 at  $\sqrt{s} = 2.125$ GeV.

The same event selection criteria and fit procedure are implemented on the other 19 data samples taken at different c.m. energies. The number of events for these samples are listed in Table II.

#### V. EXTRACTION OF THE BORN CROSS SECTION

The Born cross section is calculated by:

$$\sigma^B = \frac{N^{obs}}{\mathcal{L} \cdot (1+\delta) \cdot \epsilon \cdot \mathcal{B}},\tag{1}$$

where  $N^{obs}$  is the number of observed signal events,  $\mathcal{L}$  is the integrated luminosity,  $(1 + \delta)$  stands for  $(1 + \delta^{r}) \cdot (1 + \delta^{v}), (1 + \delta^{r})$  is initial state radiation (ISR) correction



FIG. 1: The momentum spectrum of  $K^{\pm}$  (a) and  $\pi^{\pm}$  (b), the energy spectrum of  $\gamma$  (c). The black dots with error bars are data, the hatched (green) histogram is the background from  $\phi$  sideband region, the dashed histogram is  $\phi \eta'$  MC, the solid (red) histogram is the sum of MC and the background.



FIG. 2: (color online). The fit to the  $M(\pi^+\pi^-\gamma)$  mass spectrum at  $\sqrt{s}=2.125$  GeV. The black dots with error bars are for data, the solid (red) curve for the total fit result and the dashed (blue) curve for the background from the fit.

factor, which is obtained by QED calculation [28] and 170 taking the line shape of the Born cross section measured 171 by the BABAR experiment. The vacuum polarization 172 factor  $(1 + \delta^{v})$  is taken from QED calculation with an ac-173 curacy of 0.5% [29],  $\epsilon$  is the detection efficiency including 174 reconstruction and all selection criteria,  $\mathcal{B}$  is the product 175 branching ratio and  $\mathcal{B}(\phi \to K^+K^-) \cdot \mathcal{B}(\eta' \to \pi^+\pi^-\gamma),$ 176 taken from the Particle Data Group (PDG) [26]. 177

<sup>178</sup> Both  $\epsilon$  and  $(1+\delta)$  are obtained from MC simulations of <sup>179</sup> the signal reaction at the individual c.m. energies. In the <sup>180</sup> CONEXC generator, the cross section for the ISR process <sup>181</sup>  $(\sigma_{e^+e^- \to \gamma X})$  is parameterized using

$$\sigma_{e^+e^- \to \gamma X} = \int d\sqrt{s'} \frac{2\sqrt{s'}}{s} W(s,x) \frac{\sigma^B(\sqrt{s'})}{[1 - \Pi(\sqrt{s'})]^2}, \quad (2)$$

where  $\sqrt{s'}$  is the effective c.m. energy of the final state

with s' = s(1 - x), x depends on the energy of the radiated photon according to  $x = 2E_{\gamma}/\sqrt{s}$ , W(s, x)is the radiator function and  $\Pi(\sqrt{s'})$  describes the VP effect. The latter includes contributions from leptons and quarks. The detection efficiency and the radiative correction factor depend on the input cross section, and can only be extracted by an iterative procedure, in which the line shape of the cross section from BABAR is used as the initial, and the updated Born cross section is obtained according to the simulation. We repeat the procedure until the measured Born cross section does not change by more than 0.5%.

The measured Born cross section for  $e^+e^- \rightarrow \phi \eta'$  at each energy point is listed in the Table II.

TABLE II: The Born cross sections of  $e^+e^- \rightarrow \phi \eta'$ . The center-of-mass energy  $(\sqrt{s})$ , integrated luminosity  $(\mathcal{L})$ , the yields of signal events  $(N^{obs})$ , the product of radiative correction factor and vacuum polarization factor  $(1 + \delta)$ , detection efficiency  $(\epsilon)$ , Born cross section  $(\sigma^B)$ . The first uncertainties are statistical and the second systematic.

$\sqrt{s}$ (GeV)	$\mathcal{L} (pb^{-1})$	$N^{obs}$	$(1+\delta)$	$\epsilon$	$\sigma^B$ (pb)
2.050	3.34	$4.3 \pm 3.0$	0.8878	0.2569	$39.6 \pm 27.7 \pm 4.3$
2.100	12.17	$21.3 \pm 6.3$	0.9258	0.2899	$45.8 {\pm} 13.6 {\pm} 3.8$
2.125	108.49	$267.7 {\pm} 22.2$	0.9382	0.2995	$61.7 \pm 5.1 \pm 3.9$
2.150	2.84	$12.3 \pm 4.2$	0.9483	0.3098	$103.6 {\pm} 35.4 {\pm} 6.9$
2.175	10.62	$87.4 \pm 11.0$	0.9567	0.3243	$186.3{\pm}23.4{\pm}11.6$
2.200	13.70	$105.5{\pm}11.8$	0.9640	0.3269	$171.7{\pm}19.2{\pm}10.1$
2.232	11.86	$73.6 {\pm} 10.2$	0.9720	0.3313	$135.5{\pm}18.8{\pm}11.8$
2.309	21.09	$65.6 {\pm} 9.8$	0.9772	0.3386	$66.1 {\pm} 9.9 {\pm} 4.3$
2.386	22.55	$52.7 \pm 8.8$	0.9923	0.3408	$48.6 \pm 8.1 \pm 3.8$
2.396	66.87	$163.9{\pm}15.0$	0.9939	0.3428	$50.6 {\pm} 4.6 {\pm} 3.0$
2.500	1.10	$3.7 \pm 2.1$	1.0069	0.3471	$67.8 {\pm} 38.5 {\pm} 4.5$
2.644	33.72	$73.9 {\pm} 9.5$	1.0091	0.3476	$43.9 {\pm} 5.6 {\pm} 2.4$
2.646	34.00	$50.4 \pm 8.0$	1.0093	0.3462	$29.8 {\pm} 4.7 {\pm} 1.8$
2.800	1.01	$2.0{\pm}1.4$	0.9964	0.3517	$39.8 {\pm} 27.9 {\pm} 2.4$
2.900	105.25	$113.3{\pm}12.0$	1.0110	0.3463	$21.6 \pm 2.3 \pm 1.3$
2.950	15.94	$9.9 {\pm} 3.4$	1.0130	0.3425	$12.6 {\pm} 4.3 {\pm} 0.8$
2.981	16.07	$6.9 {\pm} 2.9$	1.0124	0.3429	$8.7 {\pm} 3.7 {\pm} 0.9$
3.000	15.88	$12.6 \pm 3.7$	1.0109	0.3415	$16.2 \pm 4.7 \pm 1.2$
3.020	17.29	$14.5 \pm 4.1$	1.0080	0.3400	$17.2 {\pm} 4.9 {\pm} 1.2$
3.080	126.19	$90.2{\pm}10.3$	0.9056	0.3385	$16.4{\pm}1.9{\pm}1.0$

TABLE III: Systematic uncertainties (%) in the cross section of  $e^+e^- \rightarrow \phi \eta'$ . They are associated with the luminosity  $(\mathcal{L})$ , tracking efficiency (Tracking), photon efficiency (Photon), PID efficiency (PID), kinematic fit (Kinematic), signal and background shape (Sig. shape and Bck. shape), fit range (Range), the initial state radiation factor (ISR), the vacuum polarization correction factor (VP), mass window ( $\phi$  Cut), energy of  $\gamma$  ( $\gamma$  Cut), MC statistics (MC), branching fraction ( $\mathcal{B}$ ). The total uncertainty is obtained by summing the individual contributions in quadrature.

$\sqrt{s} \; (\text{GeV})$	L	Tracking	Photon	PID	Kinematic	Sig. shape	Bck. shape	Range	ISR	$\phi$ Cut	$\gamma$ Cut	MC	$\mathcal{B}$	Sum
2.050	1.0	3.0	1.0	3.0	3.0	0.0	0.0	8.9	0.1	0.6	2.5	0.5	2.0	10.9
2.100	1.0	3.0	1.0	3.0	2.7	0.0	0.9	5.7	0.9	0.6	1.2	0.5	2.0	8.2
2.125	1.0	3.0	1.0	3.0	2.6	0.3	0.4	1.5	0.8	0.6	2.2	0.5	2.0	6.3
2.150	1.0	3.0	1.0	3.0	2.3	0.0	0.8	1.2	0.8	1.1	3.4	0.5	2.0	6.7
2.175	1.0	3.0	1.0	3.0	2.0	1.5	0.7	2.1	1.0	1.1	0.7	0.5	2.0	6.2
2.200	1.0	3.0	1.0	3.0	2.3	0.8	1.6	1.3	0.7	0.1	0.4	0.5	2.0	5.9
2.232	1.0	3.0	1.0	3.0	2.4	1.9	1.5	1.1	0.1	6.2	0.6	0.4	2.0	8.7
2.309	1.0	3.0	1.0	3.0	1.9	2.0	2.9	0.6	0.2	0.6	1.2	0.4	2.0	6.5
2.386	1.0	3.0	1.0	3.0	1.9	2.5	4.7	1.4	0.3	0.5	1.4	0.4	2.0	7.8
2.396	1.0	3.0	1.0	3.0	1.6	0.1	2.0	0.9	0.6	1.6	1.0	0.4	2.0	6.0
2.500	1.0	3.0	1.0	3.0	1.6	0.0	2.7	2.4	0.9	2.0	0.4	0.4	2.0	6.7
2.644	1.0	3.0	1.0	3.0	0.8	0.0	0.8	0.9	0.0	2.0	0.7	0.4	2.0	5.5
2.646	1.0	3.0	1.0	3.0	0.8	0.0	1.4	1.6	0.2	1.8	1.7	0.4	2.0	6.0
2.800	1.0	3.0	1.0	3.0	0.5	0.0	0.0	0.2	0.4	3.5	0.6	0.4	2.0	6.1
2.900	1.0	3.0	1.0	3.0	0.3	1.3	0.3	1.6	0.1	3.2	0.1	0.4	2.0	6.2
2.950	1.0	3.0	1.0	3.0	0.1	1.0	0.0	2.9	0.3	0.7	1.6	0.4	2.0	6.1
2.981	1.0	3.0	1.0	3.0	0.0	0.0	0.0	5.6	0.2	7.7	2.0	0.4	2.0	10.9
3.000	1.0	3.0	1.0	3.0	0.1	0.0	0.8	0.6	0.6	5.1	0.7	0.4	2.0	7.2
3.020	1.0	3.0	1.0	3.0	0.0	0.7	2.1	0.5	0.2	4.2	0.0	0.4	2.0	6.8
3.080	1.0	3.0	1.0	3.0	0.1	0.9	2.0	1.7	1.0	0.6	0.3	0.4	2.0	5.8

## VI. SYSTEMATIC UNCERTAINTY

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Several sources of systematic uncertainties are con-<sup>228</sup> 199 sidered in the measurement of the Born cross sections.<sup>229</sup> 200 These include luminosity measurements, the differences<sup>230</sup> 201 between the data and the MC simulation for the tracking<sup>231</sup> 202 efficiency, photon's efficiency, PID efficiency, kinematic<sup>232</sup> 203 fit, the fit procedure, mass window requirement of  $\phi$ , en-<sup>233</sup> 204 ergy region of  $\gamma$ , the MC simulation of the ISR correc-<sup>234</sup> 205 tion factor and the vacuum polarization factor, as well as<sup>235</sup> 206 uncertainties in the branching fractions of intermediate<sup>236</sup> 207 237 state decays and in the luminosity measurements. 208

(a) Luminosity: The integrated luminosity of the data<sup>238</sup>
samples used in this analysis are measured using large an-<sup>239</sup>
gle Bhabha events, and the corresponding uncertainties<sup>240</sup>
are estimated to be 1.0% [30].

(b) Tracking: The uncertainty of the tracking effi-<sup>242</sup> ciency is investigated using a control sample of  $e^+e^- \rightarrow^{243}$  $K^+K^-\pi^+\pi^-$  process [6]. The difference in tracking effi-<sup>244</sup> ciency between the data and the MC simulation is esti-<sup>245</sup> mated to be 1% per track. Hence, 3.0% is taken as the<sup>246</sup> systematic uncertainty for the three selected kaons.

(c) *Photon:* The uncertainty due to photon detection<sup>248</sup> 1% per photon [31].

(d) *PID*: To estimate the PID efficiency uncertainty,<sup>250</sup> we study  $K^{\pm}$  and  $\pi^{\pm}$  PID efficiencies with the same con-<sup>251</sup> trol samples as those used in the tracking efficiency. The<sub>252</sub> average PID efficiency difference between the data and<sub>253</sub> the MC simulation is found to be 1% per charged track<sub>254</sub>

and taken as a systematic uncertainty. Therefore, 3.0% is taken as the systematic uncertainty for the three selected kaons.

(e) Kinematic fit: Uncertainty associated with kinematic fits come from the inconsistency of the track helix parameters between the data and the MC simulation. The helix parameters for the charged tracks of MC samples are corrected to eliminate the inconsistency, as described in Ref. [32], and the agreement of  $\chi^2$  distributions between the data and the MC simulation is much improved. We take he differences on the selection efficiencies with and without the correction as the systematic uncertainties.

(f) Mass window of  $\phi$ : A mass window requirement on the  $K^+K^-$  invariant-mass introduces a systematic uncertainty on the efficiency. The difference between  $|M(K^+K^-) - M(\phi)| \leq 0.015$  GeV and  $|M(K^+K^-) - M(\phi)| \leq 0.020$  GeV is worked as uncertainty.

(g) Energy of  $\gamma$ : The difference in the efficiency between  $E(\gamma) > 0.07$  GeV and  $E(\gamma) > 0.06$  GeV is worked as uncertainty.

(h) Fitting procedure: Fit to the invariant-mass of  $\pi^+\pi^-\gamma$  to extract the signal yields of  $e^+e^- \rightarrow \phi \eta'$  process. The following three aspects are considered when evaluating the systematic uncertainty associated with the fit procedure.

(1) Fitting range: In the fit, the  $M(\pi^+\pi^-\gamma)$  is fitted by varying the fitting range from (0.85, 1.05) GeV/ $c^2$ to (0.8, 1.10) GeV/ $c^2$ . The difference in the yield are

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<sup>255</sup> treated as the systematic uncertainty from the fit range.

(2) Signal shape: In the fit, the signal shape is de-256 scribed by a shape obtained from a MC simulation convo-257 luted with a Gaussian function. The uncertainty related 258 to the signal line shape is estimated with an alternative fit 259 using the same function for signal line-shape, but fixing 260 width of Gaussian function to the value by changing one 261 standard deviation of width obtained in the nominal fit. 262 263 The difference of the yields between them is considered as the systematic uncertainty from the signal shape. 264

(3) Background shape: In the fit, the background shape
is described as a second-order polynomial function. The
fit with a third-order polynomial function for the background shape is used to estimate its uncertainty.

(i) ISR factor: The cross section is measured by it-<sup>296</sup> erating until  $(1 + \delta^r) \times \epsilon$  converges, and the difference<sup>297</sup> between the last two iterations is taken as the systematic<sup>298</sup> uncertainty associated with the ISR correction factor.

(j) Branching fraction: The uncertainties in the<sub>301</sub> branching fractions for the processes  $\phi \to K^+K^-$  and  $\pi' \to \pi^+\pi^-\gamma$  are taken from the PDG [26].

 $_{276}$  (k) *MC:* The uncertainty is estimated by the number  $_{304}^{303}$  of the generated events.

Assuming all of the above systematic uncertainties,<sup>306</sup> shown in Table III, are independent, the total system-<sup>307</sup> atic uncertainties are obtained by adding the individual<sup>308</sup> uncertainties in quadrature. <sup>309</sup>

#### 282 VII. RESONANCE IN THE LINE SHAPE OF 283 CROSS SECTION OF $e^+e^- \rightarrow \phi \eta'$

Figure 3 shows the measured Born cross section for<sup>316</sup> 284  $e^+e^- \rightarrow \phi \eta'$  over the energy region studied in this work.<sup>317</sup> 285 There is a clear structure around 2.200 GeV. To study the<sup>318</sup> 286 possible resonant structure in the  $e^+e^- \rightarrow \phi \eta'$  process, 287 a  $\chi^2$  fit incorporating the correlated and uncorrelated 288 uncertainties is performed to the measured cross section. 289 Assuming that the  $\phi \eta'$  signals come from a resonance 290 decay, we fit the line shape using a coherent sum of a 291 phase-space modified Breit-Wigner (BW) function with 292 a mass-dependent width and a phase-space term. The 293 probability density function (PDF) is parameterized as 294

$$|A(\sqrt{s})|^{2} = |C_{0}\sqrt{\Phi(\sqrt{s})} + e^{i\varphi} \times BW(\sqrt{s})|^{2}, \quad (3)$$

$$BW(\sqrt{s}) = \frac{M_R}{\sqrt{s}} \frac{\sqrt{12\pi\Gamma_{e^+e^-}^R \mathcal{B}_R(\phi \ \eta')\Gamma_{tot}^R}}{s - M_R^2 + iM_R\Gamma_{tot}^R} \cdot \sqrt{\frac{\Phi(s)}{\Phi(M_R)}}$$
(4)

$$\Phi(\sqrt{s}) = \frac{\sqrt{[s - (m_{\eta'} + m_{\phi})^2][s - (m_{\eta'} - m_{\phi})^2]}}{2 \cdot s} \quad (5)$$

$$\Phi(M) = \frac{\sqrt{[M_R^2 - (m_{\eta'} + m_{\phi})^2][M_R^2 - (m_{\eta'} - m_{\phi})^2]}}{2 \cdot M_R^2}$$
(6)

where  $M_R$  is the mass of the resonance,  $\Gamma_{tot}^R$  the total width,  $\Gamma_{e^+e^-}^R$  the  $e^+e^-$  partial width,  $\mathcal{B}_{\mathcal{R}}(\phi \eta')$  the branch fraction of the resonance decay to  $\phi \eta'$ ,  $\varphi$  the phase angle between the resonance and the phase-space contribution,  $\Phi(\sqrt{s})$  the phase space factor for and Swave two-boday system.  $m_{\eta'}$  and  $m_{\phi}$  is the mass of  $\eta'$ and  $\phi$ , respectively.

The fit has two solutions with equally good fit quality,  $\chi^2/ndf = 27.73/15$ , and identical masses, widths of the resonances and the product of the electronic widths with the branching fractions, while the phases are different. The mass and width of the resonance are determined to be  $M = (2182.4 \pm 5.1) \text{ MeV}/c^2$  and  $\Gamma = (142.2 \pm 16.6)$ MeV, where the error is statistical only. Figure 3 shows the fit result and the parameters of the resonance are summarized in Table IV. The resonance has a mass consistent with that of  $\phi(2170)$  within 1.0  $\sigma$ . However, its measured width is much larger than the average width,  $83\pm 12$  MeV, of the  $\phi(2170)$ . The significance of the resonance is determined to be  $12.47\sigma$  (including systematic uncertainties) by comparing the change of  $\Delta(\chi^2)$  with and without the R amplitude in the fit and taking the change of number of degree of freedom  $\Delta n.d.f = 4$  into account.

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FIG. 3: The fit of cross section line shape of  $e^+e^- \rightarrow \phi \eta'$  is obtained by the Probability Density Function 3 in this work.

TABLE IV: Results of the fit to the  $e^+e^- \rightarrow \phi \eta'$  cross section. The error is statistical only.

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Parameters	Solution I Solution II
$M_R \; ({\rm MeV}/c^2)$	$2182.4 \pm 5.1$
$\Gamma^R_{tot}$ (MeV)	$142.2 \pm 16.6$
$\mathcal{B}_{\mathcal{R}}\Gamma^{R}_{e^{+}e^{-}}(\text{keV})$	$0.0073 \pm 0.0016$
$\varphi(\mathrm{rad})$	$2.9755 \pm 0.4502$ $-0.1662 \pm 0.4473$

# A. Systematic Uncertainty for resonance parameters

The systematic uncertainties of the resonant parameters in the fit to the energy-dependent cross section of  $e^+e^- \rightarrow \phi \eta'$  are mainly from the uncertainties of c.m. energy determination, energy spread, the cross section measurement and the parametrization of the BW function.

326	• Energy scale: The uncertainty from the c.m.	en-362
327	ergy measurement is studied by taking the un	cer-363
328	tainty of the c.m. energy 1.6 MeV at 2.125 GeV	34 364
329	into consideration. This common uncertainty	will <sub>365</sub>
330	propagate only to the masses of the resonance v	vith366
331	the same amount, i.e., $\pm 1.6 \text{ MeV}c^2$ .	367

#### • Energy spread:

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To estimate the uncertainty from the energy<sub>370</sub> spread, the PDF convoluted with a Gaussian func-<sub>371</sub> tion with a resolution of 1.6 MeV [35] is used to<sub>372</sub> fit the data, and the uncertainty is estimated by<sub>373</sub> comparing the results with the nominal ones. <sub>374</sub>

#### 338 VIII. SUMMARY AND DISCUSSION

In summary, based on data samples collected with the<sub>380</sub> 339 BESIII detector at the BEPCII collider at 20 c.m. ener-381 340 gies from 2.050 to 3.080 GeV, we perform a precise cross<sub>382</sub> 341 section measurement of  $e^+e^- \rightarrow \phi \eta'$ . By assuming the<sub>383</sub> 342  $\phi \eta'$  come from a single resonance, we extract the mass<sub>384</sub> 343 and width of the resonance to be  $2180.3 \pm 4.9$  MeV and 385 344  $140.1 \pm 16.4$  MeV, respectively. Here, the first errors are 336 345 statistical and the second ones are systematic. Its statis-387 346 tical significance is estimated to be large than 12.0  $\sigma$ . 388 347

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Considering the conservation laws,  $J^{PC}$  of the resonance is equal to be 1<sup>--</sup>. Due to its mass comparable to the  $\phi(2170)$ , the resonance agrees with the  $\phi(2170)$  resonance reported by previous experiments. However, our measured width is much larger than the  $\phi(2170)$  average width reported by previous experiments. If we assume it is the same resonance as the  $\phi(2170)$ , a new decay channel of  $\phi(2170) \rightarrow \phi \eta'$  has been observed first time.

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